## YEAR 9 - REASONING WITH NUMBER

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## Numbers

 $\bigcirc$  = 1

The act of counters

into their

negative is turning

them over

b = -4

#### What do I need to be able to do?

By the end of this unit you should be able to:

- Identify integers, real and rational numbers
- Work with directed number
- Solve problems with number
- Find HCF/ LCM
- Odd/ Subtract fractions
- Multiply/ Divide fractions
- Write numbers in standard form

#### Keywords

Integer: a whole number that is positive or negative

Rational: a number that can be made by dividing two integers

Irrational: a number that cannot be made by dividing two integers

**Inverse operation**: the operation that reverses the action

Quotient: the result of a division

**Product**: the result of a multiplication.

Multiples: found by multiplying any number by positive integers

Factor: integers that multiply together to get another number

#### Integers, real and rational numbers

Rational — root word: ratio

**Real numbers**:  $\frac{2}{3}$  stems from 2:1 ( $\frac{2}{3}$  of the whole)

Irrational numbers:  $\sqrt{2}$  the solution is a decimal that never ends and does not repeat.

The square root of a negative is not a real number and cannot be found



Common factors are factors two or more numbers share

HCF — Highest common factor

HCF of 18 and 30



#### LCM — Lowest common multiple

LCM of 9 and 12

9, 18, 27, 36, 45, 54

12, 24, 36, 48, 60

I CM = 36

The first time their multiples match

#### Standard form

any number A x 10 n between I and

less than 10



= 600000 + 800000

= 1400000

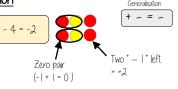
 $15 \div 0.3 \times 10^5 \div 10^3$ 

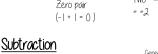
 $(1.5 \times 10^5) \div (0.3 \times 10^3)$ 

= 1.4 x 10<sup>5</sup>

 $=5 \times 10^{2}$ 

#### Directed number **Oddition**

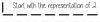










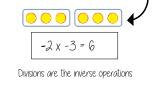


## Generalisation



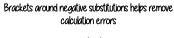


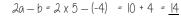


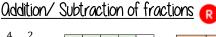


a = 5

Multiplication









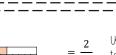
Shade in 3





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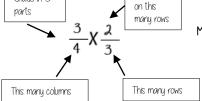
Repeat it



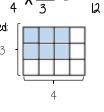


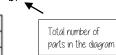
denominators

#### Multiplication/Division of fractions 🔞







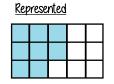


Parts shaded

#### Remember to use reciprocals









## YEAR 9 - REASONING WITH NUMBER...

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## Using Percentages

## What do I need to be able to do?

#### By the end of this unit you should be able to:

- Use FDP equivalence
- Calculate percentage increase and decrease
- Express percentage change
- Solve reverse percentage problems
- Solve percentage problems (calculator and non calculator problems)

#### Keywords

Percent: parts per 100 — written using the 🗸 symbol

**Decimal:** a number in our base 10 number system. Numbers to the right of the decimal place are called decimals. **Fraction:** a fraction represents how many parts of a whole value you have.

**Equivalent**: of equal value.

Reduce: to make smaller in value.

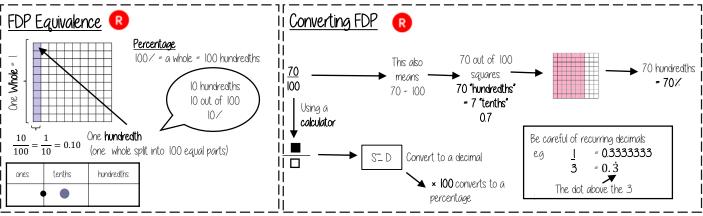
Growth: to increase / to grow.

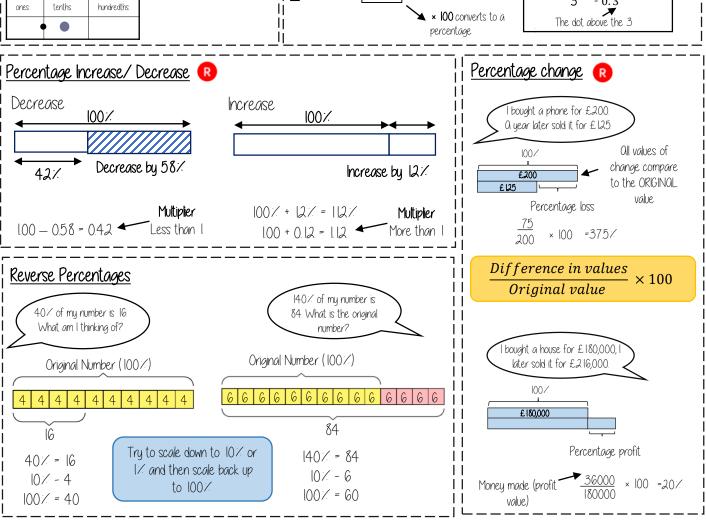
Integer: whole number, can be positive, negative or zero.

Invest: use money with the goal of it increasing in value over time (usually in a bank).

Multiplier: the number you are multiplying by.

| **Profit**: the income take away any expenses/ costs.





## YEAR 9 - REASONING WITH NUMBER.

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## Maths & Money

## What do I need to be able to do?

#### By the end of this unit you should be able to:

- Solve problems with bills and bank statements
- Calculate simple interest
- Calculate compound interest
- Calculate wages and taxes
- Solve problems with exchange rates
- Solve unit pricing problems

#### Keywords

Credit: money being placed into a bank account

**Debit**: money that leaves a bank account

Balance: the amount of money in a bank account

Expense: a cost/outgoing.

Deposit: an initial payment (often a way of securing an item you will later pay for)

Multiplier: a number you are multiplying by (Multiplier more than I = increasing, less than I = decreasing)

Per Onnum: each year

Currency: the type of money a country uses.

**Unitary**: one — the cost of one.

#### Bills and Bank Statements

Bills — tell you the amount items cost and can show how

much money you need to pay.

Some can include a total

Some can include a total	11010	
Some can include a local	N.A.II	
Look for different units	Milk	
(Is it in pence or pounds)	Tea	

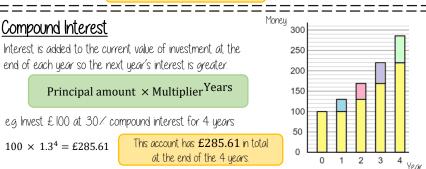
<u>ents</u> s cost and can show how			
Menu	Price		
Milk	89p		
Tea	£1.50		

#### Bank Statements

Bank statement can have negative balances if the money spent is higher than the money coming into the account

Date	Description	Credit	Debit	Balance
l9th Sept	Salary	£1500		£1500
l9th Sept	Mortgage		£600	£900
25 <sup>th</sup> Setp	Bday Money	£15		£915

# Simple Interest For each year of investment the interest remains the same Principal amount ×Interest Rate × Years 100 Principal amount is the amount invested in the account. e.g. hvest £ 100 at 30 / simple interest for 4 years 100 × 30 × 4



#### Value Odded Tax (VOT)

VOT is payable to the government by a business. In the UK VOT is 20% and added to items that are bought.

Essential items such as food do not include VOT.

#### Wages and Taxes

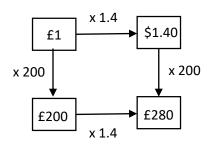
Salaries fall into tax brackets — which means they pay this much each month from their salary.

Taxable Income	Tax Rate
£12 501 to £50 000	20%
£50 001 to £150 000	40%
over £150 000	45%

Over time:

Time and a half — means 1.5 times their hourly rate





When making estimates it is also useful to use <u>estimates</u> to check if our solution is reasonable.

Use inverse operations to reverse the exchange process

Common Currencies		
United Kingdom	£	Pounds
United States of Omerica	\$	Dollars
Europe	€	Euros

#### Unit Pricing

4 Oranges £1 5 cupcakes £1.20

4 = £1.00  $\div 2$  5 = £1.20  $\div 5$ 1 = £0.25  $\div 2$  1 = £0.20

3 + 2 = £0.20

To calculate unit per cost you divide by the cost.

Cupcakes are the best value as one item has the cheapest value

There is a directly proportional relationship between the cost and number of units

## YEAR 9 - REASONING WITH GEOMETRY

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## Deduction

#### What do I need to be able to do?

#### By the end of this unit you should be able to:

- Identify angles in parallel lines
- Solve anale problems
- Make conjectures with angles
- Make conjectures with shapes

#### Keywords

Parallel: two straight lines that never meet with the same gradient.

Perpendicular: two straight lines that meet at 90°

Transversal: a line that crosses at least two other lines.

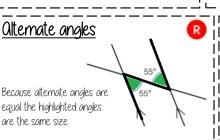
Sum: the result of adding two or more numbers.

Conjecture: a statement that might be true but is not proven.

Equation: a statement that says two things are equal

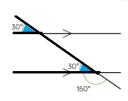
Polygon: a 2D shape made from straight edges.

Counterexample: an example that disproves a statement

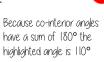


#### ¦¦ <u>Corresponding angles</u>

Because corresponding angles are equal the highlighted angles are the



#### R : Co-interior angles

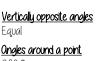


Ois angles on a line add up to 180° co-interior angles can also be calculated from applying alternate/corresponding

#### Solving angle problems

#### Ongles on a straight Line

1800







Form an equation

$$2x + 4x = 180^{\circ}$$

#### State the reason

The sum of anales on a straight line is 180°

 $2x + 4x = 180^{\circ}$ 

 $6x = 180^{\circ}$ 

 $x = 30^{\circ}$ 

#### Interior Ongles

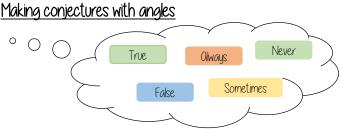
The angles enclosed by the polygon

(number of sides -2) x 180

#### <u>Triangles</u>

Sum of angles is 180 °

Isosceles have the same



#### Proving a conjecture

a pattern is noticed for many cases

#### Disproving a conjecture

Only one counterexample is needed to disprove a conjecture







#### Apply the angle rules

The sum of angles in a triangle is 180°

#### Test the theory 180 - 70 - 20 = 90

$$180 - 85 - 5 = 90$$

180 - 45 - 45 = 90

#### Make conjecture

The anale that meets the circumference in a semi circle is 90

#### Making conjectures with shapes

#### Keywords and facts to recall with shape

Orea: the amount of space inside a shape Perimeter: the length around a shape Regular Polygons: All sides and angles are equal

#### Quadrilateral Facts



Oll sides equal size Oll anales 90°





#### <u>Parallelogram</u>

Opposite sides are parallel Opposite angles are equal Co-interior angles



#### Rhombus

Oll sides equal size Opposite angles are equal



#### Kite

No parallel lines Equal lengths on top sides Equal lengths on bottom One pair of equal angles

# YEAR 9 — REASONING WITH GEOMETRY... Rotation & Translation

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#### What do I need to be able to do?

#### By the end of this unit you should be able to:

- Identify the order of rotational symmetry
- Rotate a shape about a point on the
- Rotate a shape about a point not on a
- Translate by a given vector
- Compare rotations and reflections

#### Keywords

Rotate: a rotation is a circular movement

Symmetry: when two or more parts are identical after a transformation.

Reaular: a regular shape has angles and sides of equal lengths. **Invariant**: a point that does not move after a transformation.

Vertex: a point two edges meet. Horizontal: from side to side

Vertical: from up to down

### Rotational Symmetry



Tracing paper helps check rotational symmetry

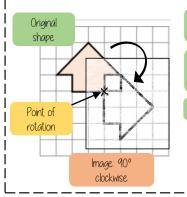
I. Trace your shape (mark the centre point)

2. Rotate your tracing paper on top of the original through 360°

3. Count the times it fits back into itself

O regular pentagon has rotational symmetry of order 5

#### Rotate from a point (in a shape)



I. Trace the original shape (mark the point of rotation)

2 Keep the point in the same place and turn the tracing

3. Draw the new shape





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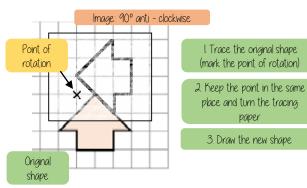
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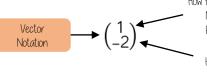
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#### Rotate from a point (outside a shape)

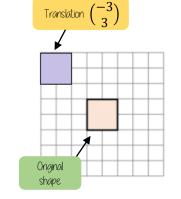


#### Translation and vector notation



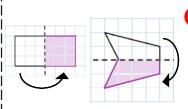
How far left or right to move Negative value (left) Positive value (right)

> How far up or down to move Negative value (down) Positive value (up)



Every vertex has been translated by the same amount

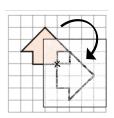
#### Compare rotations and reflections



Reflections are a mirror image of the original shape.

Information needed to perform a reflection

- Line of reflection (Mirror line)



Rotations are the movement of a shape in a circular motion

#### Information needed to perform a rotation:

- Point of rotation
- Direction of rotation
- Degrees of rotation