YEAR 9 - REASONING WITH ALGEBRA

@whisto maths

Straight Line Graphs

What do I need to be able to do?

By the end of this unit you should be able to:

- Compare gradients
- Compare intercepts
- Understand and use y= mx + c
- Find the equation of a line from a graph
- Interpret gradient and intercepts of reallife graphs

Keywords

Gradient: the steepness of a line

Intercept: where two lines cross. The y-intercept: where the line meets the y-axis.

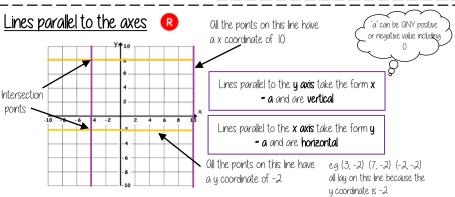
Parallel two lines that never meet with the same gradient.

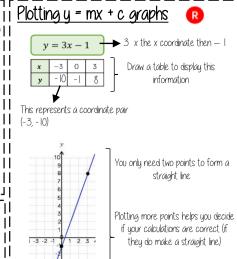
Co-ordinate: a set of values that show an exact position on a graph.

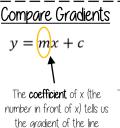
Linear: linear graphs (straight line) — linear common difference by addition/subtraction

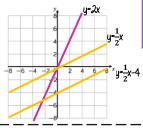
Osymptote: a straight line that a graph will never meet. Reciprocal: a pair of numbers that multiply together to give 1.

I I Perpendicular: two lines that meet at a right angle





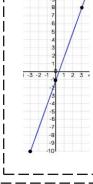




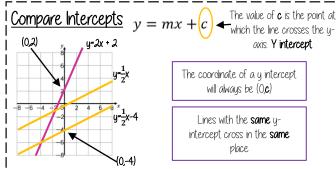
The **areater** the gradient — the steeper the line

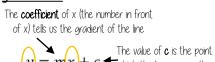
> Parallel lines have the same gradient

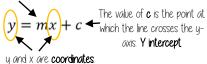
Softing a copper



Remember to join the points to make







can be rearranged: E.g.: u = c + mx c = y - mxIdentify which coefficient you are identifying or

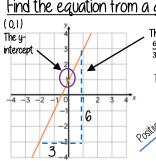
The u-intercept shows the

minimum charge.

The gradient represents the price per mile

The equation of a line

Find the equation from a graph



The Gradient $\frac{6}{2} = 2$

v = 2x + 1

The direction of the line indicates a positive

Negative gradients

Real life graphs

y = mx + c

A plumber charges a £25 callout fee, and then £12.50 for every hour. Complete the table of values to show the cost of hiring the plumber.

In real life graphs like this values will always be positive because they

measure distances or objects which cannot be negative

When you have 0 pens this has 0 cost. The gradient shows the

Direct Proportion graphs

A box of pens costs £2.30

Complete t	ne table of	values to sn	iow the cost	or buying t	poxes of per
Boxes	0	1	2	3	8
Cost (£)		£2.30			

To represent direct proportion the graph must start at the origin.

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Forming and Solving Equations

What do I need to be able to do?

By the end of this unit you should be able to:

- Solve inequalities with negative numbers
- Solve equations with unknowns on both sides |
- Solve inequalities with unknowns on both
- Substitute into formulae and equations
- Rearrange formulae

!!Keuwords

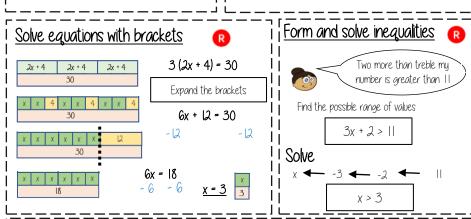
Inequality: an inequality compares who values showing if one is greater than, less than or equal to another

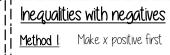
Variable: a quantity that may change within the context of the problem

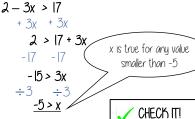
Rearrange: Change the order

Inverse operation: the operation that reverses the action

Substitute: replace a variable with a numerical value Solve: find a numerical value that satisfies an equation

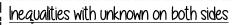




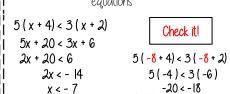


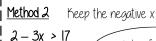
2 - 3(-6) = 20TRUE/ CORRECT

true...



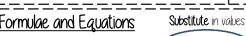
Solving inequalities has the same method as equations





x > -5

x is true for any value bigger than -5 -3x > 15÷-3 This cannot be



Equations with unknown on both sides

Formulae — all expressed in symbols

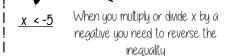
4x + 5 = 3x + 24

x + 5 = 24

x = 19

-3x

Equations — include numbers and can be solved |



Rearranging Formulae (one step)



X = y + Z

Rearrange to make y the subject.

y = x - Z

→⁺Z —

Rearranging can also be checked by substitution.

Language of rearranging...

Make XXX the subject

Using inverse operations or fact families will guide you through rearranging formulae

Rearrange

Change the subject

Rearranging Formulae (two step)

Ш

In an equation (find x)

4x - 3 = 9

-20 IS smaller than -18

In a formula (make x the subject) xy - s = a

+3 4x = 12

+ 5 + 5 xu = a + s÷ y ÷ y $X = \alpha + S$

The steps are the same for solving and rearranging Rearranging is often needed when using y = mx + c

e.g. Find the gradient of the line 2y - 4x = 9

Make y the subject first y = 4x + 9

Gradient = 4= 2

YEAR 9 - REASONING WITH ALGEBRA

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Testing conjectures

What do I need to be able to do?

By the end of this unit you should be able to:

- Use factors, multiples and primes
- Reason True or False
- Reason Olwaus, sometimes never true
- Show that reasoning
- Make conjectures about number
- Expand binomials
- Make conjectures with algebra
- Explore the 100 arid

Keywords

Multiples: found by multiplying any number by positive integers Factor: integers that multiply together to get another number.

Prime: an integer with only 2 factors.

HCF: highest common factor (biggest factor two or more numbers share)

LCM: lowest common multiple (the first time the times table of two or more numbers match)

Verify: the process of making sure a solution is correct

Proof: logical mathematical arguments used to show the truth of a statement

Binomial a polynomial with two terms

Quadratic: a polynomial with four terms (often simplified to three terms)

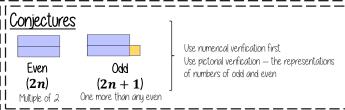
Factors, Multiples and Primes HCF — Highest common factor Multiplication part-whole models HCF of 18 and 30 1, 2, 3, 6, 9, 18 30 1, 2, 3, 5, 6, 10, 15, 30 Common factors are factors two or more numbers share LCM - Lowest common multiple LCM of 9 and 12 9, 18, 27, 36, 45, 54 Oll three prime factor trees represent the 12, 24, 36, 48, 60 same decomposition Common multiples are multiples two or more numbers share 📙



No example supports the statement



Compare the left hand side of an equation with the

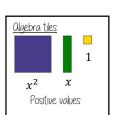


right hand side — are they the same or different?

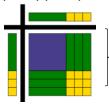
Expandina binomials $2(x+2) \equiv 2x+4$



Olgebra tiles can represent a binomial expansion Has two terms



$$(x+3)(x+3) \equiv x^2 + 6x + 9$$



This is a quadratic. It has four terms which simplified to three terms

The order of the binomial has no impact on the outcome eg (x + 3)(3 + x)

Exploring the 100 square

In terms of n' is used to make generalisations about relationships between numbers

Positions of numbers in relation to n form expressions. E.g. one space to the right of n

n + 1

E.g. One row below nn + 10

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

Examples to try

0 and 1

Fractions

Negative

numbers

The size of the grid for generalisation changes the relationship statements

YEAR 9 — CONSTRUCTING IN 2D/3D...

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3D Shapes

What do I need to be able to do?

By the end of this unit you should be able to:

- Name 2D & 3D shapes
- Recognise Prisms
- Sketch and recognise nets
- Draw plans and elevations
- Find areas of 2D shapes
- Find Surface area for cubes, cuboids, triangular prisms and culinders
- Find the volume of 3D shapes

Keywords

2D: two dimensions to the shape e.g. length and width

3D: three dimensions to the shape e.g. length, width and height

Vertex: a point where two or more line segments meet

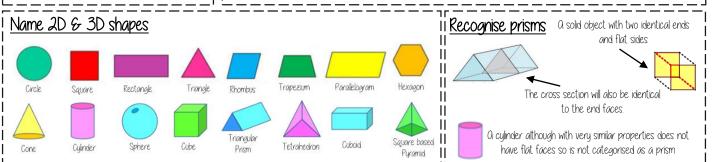
Edge a line on the boundary joining two vertex

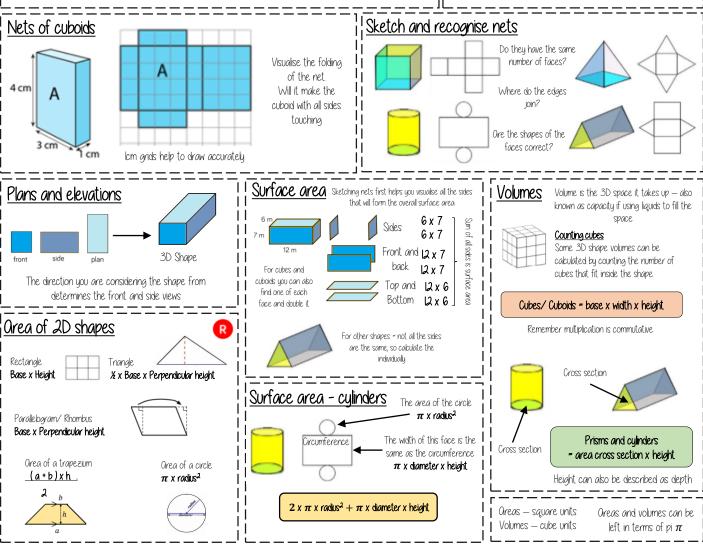
Face: a flat surface on a solid object

Cross-section: a view inside a solid shape made by cutting through it

Plan: a drawing of something when drawn from above (sometimes birds eye view)

Perspective: a way to give illustration of a 3D shape when drawn on a flat surface.





YEAR 9 - CONSTRUCTING IN 2D/3D.

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Constructions & congruency

What do I need to be able to do?

By the end of this unit you should be able to:

- Draw and measure angles
- Construct scale drawings
- Find locus of distance from points, lines, two
- Construct perpendiculars from points, lines, anales
- Identify congruence
- Identify congruent triangles

Keywords

Protractor: piece of equipment used to measure and draw angles

Locus: set of points with a common property

Eauidistant: the same distance

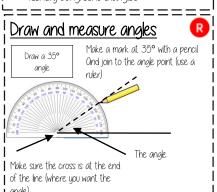
Discorectanale: (a stadium) — a rectangle with semi circles at either end

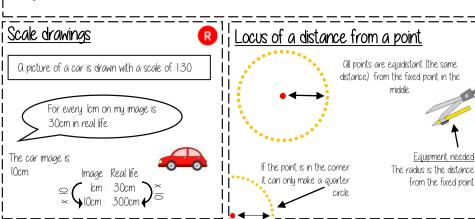
Perpendicular: lines that meet at 90°

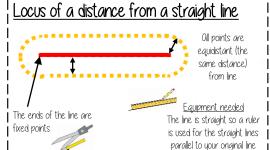
arc: part of a curve

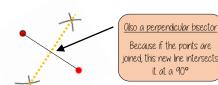
Bisector: a line that divides something into two equal parts

Congruent: the same shape and size







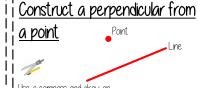


Locus equidistant from two points

joined, this new line intersects



Join the intersections with a Keep the compass the same Oll points on this line are size and draw two arcs from equidistant from both points



Equipment needed

from the fixed point

Use a compass and draw an arc that cuts the line. Use the point to place the compass

Keep the compass the same distance and now use uour new points to make new interconnecting arcs

Connectina the arcs makes the bisector

ocus of a distance from two lines



Keep the compass the same size and use

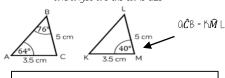
intersecting arcs in the middle Join the vertex to the intersection

Conaruent fiaures

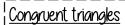


Congruent figures are identical in size and shape — they can be reflections or rotations of each

Congruent shapes are identical — all corresponding sides and angles are the same size



Because all the angles are the same and OC=KM BC=LM trianales OBC and KLM are congruent



Side-side-side

Oll three sides on the triangle are the same size

Ongle-side-angle

Two angles and the side connecting them are equal in two triangles

Side-angle-side

Two sides and the angle in-between them are equal in two triangles (it will also mean the third side is the same size on both shapes)

Right angle-hypotenuse-side

II The triangles both have a right angle, the hypotenuse and one side are the same

