YEAR 9 - REASONING WITH NUMBER

@whisto maths

Numbers

 \bigcirc = 1

The act of counters

into their

negative is turning

them over

b = -4

Parts shaded

Total number of

parts in the diagram

What do I need to be able to do?

By the end of this unit you should be able to:

- Identify integers, real and rational numbers
- Work with directed number
- Solve problems with number
- Find HCF/ LCM
- Odd/ Subtract fractions
- Multiply/ Divide fractions
- Write numbers in standard form

Keywords

Integer: a whole number that is positive or negative

Rational: a number that can be made by dividing two integers

Irrational: a number that cannot be made by dividing two integers

Inverse operation: the operation that reverses the action

Quotient: the result of a division

Product: the result of a multiplication.

Multiples: found by multiplying any number by positive integers

Factor: integers that multiply together to get another number

Integers, real and rational numbers

Rational — root word: ratio

Real numbers: $\frac{2}{3}$ stems from 2:1 ($\frac{2}{3}$ of the whole)

Irrational numbers: $\sqrt{2}$ the solution is a decimal that never ends and does not repeat.

The square root of a negative is not a real number and cannot be found

HCF/LCM 🔞 I is a common factor of all

Common factors are factors two or more numbers share

HCF — Highest common factor

HCF of 18 and 30



LCM — Lowest common multiple

LCM of 9 and 12

9, 18, 27, 36, 45, 54

12, 24, 36, 48, 60

I CM = 36

The first time their multiples match

Standard form

any number A x 10 n between I and less than 10



= 600000 + 800000

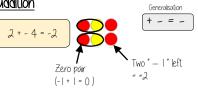
= 1.4 x 10⁵

 $(1.5 \times 10^5) \div (0.3 \times 10^3)$ $15 \div 0.3 \times 10^5 \div 10^3$

= 1400000

 $=5 \times 10^{2}$

Directed number **Oddition**









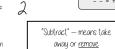




Shade in 3

Generalisation





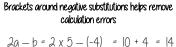


a = 5

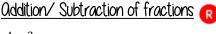
-2x-3=6

Divisions are the inverse operations

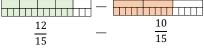
Multiplication



$$2a - b = 2 \times 5 - (-4) = 10 + 4 = 14$$

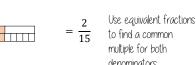




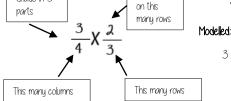


Repeat it

========



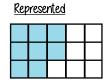
Multiplication/Division of fractions 🔞



Remember to use reciprocals









YEAR 9 - REASONING WITH NUMBER...

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Using Percentages

What do I need to be able to do?

By the end of this unit you should be able to:

- Use FDP equivalence
- Calculate percentage increase and decrease
- Express percentage change
- Solve reverse percentage problems
- Solve percentage problems (calculator and non calculator problems)

Keywords

Percent: parts per 100 — written using the % symbol

Decimal: a number in our base 10 number system. Numbers to the right of the decimal place are called decimals. **Fraction:** a fraction represents how many parts of a whole value you have.

ı **ı Equivalent**: of equal value.

Reduce: to make smaller in value.

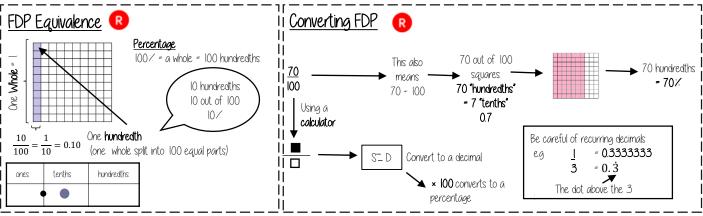
Growth: to increase / to grow.

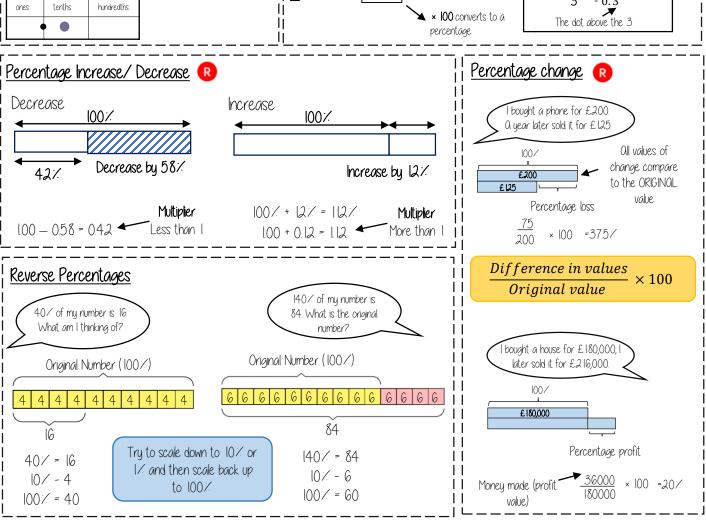
Integer: whole number, can be positive, negative or zero.

Invest: use money with the goal of it increasing in value over time (usually in a bank).

Multiplier: the number you are multiplying by.

| **Profit**: the income take away any expenses/ costs.





YEAR 9 - REASONING WITH NUMBER.

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Maths & Money

What do I need to be able to do?

By the end of this unit you should be able to:

- Solve problems with bills and bank statements
- Calculate simple interest
- Calculate compound interest
- Calculate wages and taxes
- Solve problems with exchange rates
- Solve unit pricing problems

<u>Keywords</u>

Credit: money being placed into a bank account

Debit: money that leaves a bank account **Balance**: the amount of money in a bank account

Expense: a cost/outgoing.

Deposit: an initial payment (often a way of securing an item you will later pay for)

Multiplier: a number you are multiplying by (Multiplier more than I = increasing, less than I = decreasing)

Per Onnum: each year

Currency: the type of money a country uses.

Unitary: one — the cost of one.

Bills and Bank Statements

<u>Bills</u> — tell you the amount items cost and can show how

much money you need to pay.

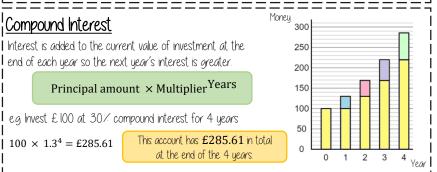
Some can include a total	Menu	Price
Look for different units	Milk	89p
ls it in pence or pounds)	Tea	£1.50

Bank Statements

Bank statement can have negative balances if the money spent is higher than the money coming into the account

Date	Description	Credit	Debit	Balance
l ^{qth} Sept	Salary	£1500		£1500
l9th Sept	Mortgage		£600	£900
25 th Setp	Bday Money	£15		£915

Simple Interest For each year of investment the interest remains the same Principal amount ×Interest Rate × Years 100 Principal amount is the amount invested in the account. 1 e.g. Invest £ 100 at 30 / simple interest for 4 years 100 × 30 × 4



<u>Value Odded Tax (VOT)</u>

VOT is payable to the government by a business. In the UK VOT is 20% and added to items that are bought.

Essential items such as food do not include VOT.

Wages and Taxes

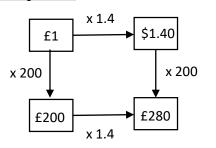
Salaries fall into tax brackets — which means they pay this much each month from their salary.

Taxable Income	Tax Rate
£12 501 to £50 000	20%
£50 001 to £150 000	40%
over £150 000	45%

Over time:

Time and a half — means 1.5 times their hourly rate





When making estimates it is also useful to use <u>estimates</u> to check if our solution is reasonable.

Use inverse operations to reverse the exchange process

Common Currencies		
United Kingdom	£	Pounds
United States of America	\$	Dollars
Europe	€	Euros

Unit Pricing

4 Oranges £1 5 cupcakes £1.20

4 = £1.00 $\div 2$ 5 = £1.20 $\div 5$ 1 = £0.25 $\div 2$ 1 = £0.20

 $3 \cancel{\cancel{\hspace{-0.05cm} }} \div 2 \qquad 1 = £0.20$

To calculate unit per cost you divide by the cost.

Cupcakes are the best value as one item has the cheapest value

There is a directly proportional relationship between the cost and number of units.

YEAR 9 - REASONING WITH GEOMETRY

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Deduction

What do I need to be able to do?

By the end of this unit you should be able to:

- Identify angles in parallel lines
- Solve anale problems
- Make conjectures with angles
- Make conjectures with shapes

Keywords

Parallel: two straight lines that never meet with the same gradient.

Perpendicular: two straight lines that meet at 90°

Transversal: a line that crosses at least two other lines.

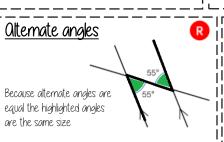
Sum: the result of adding two or more numbers.

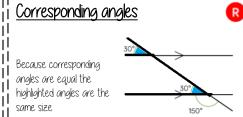
Conjecture: a statement that might be true but is not proven.

Equation: a statement that says two things are equal

Polygon: a 2D shape made from straight edges.

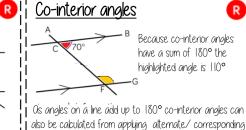
Counterexample: an example that disproves a statement

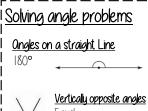




Form an equation

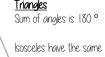
 $2x + 4x = 180^{\circ}$

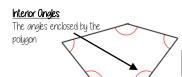






Link angle facts to algebra





State the reason

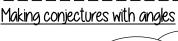
The sum of anales on a

straight line is 180°

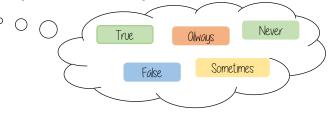
 $2x + 4x = 180^{\circ}$ $6x = 180^{\circ}$

 $x = 30^{\circ}$

(number of sides -2) x 180



Ongles around a point



Proving a conjecture a pattern is noticed for

Apply the angle rules

The sum of

angles in a

triangle is 180°

Disproving a conjecture Only one counterexample is needed to







Make conjecture

180 - 70 - 20 = 90180 - 85 - 5 = 90180 - 45 - 45 = 90

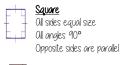
The anale that meets the circumference in a semi circle is 90

Making conjectures with shapes

Keywords and facts to recall with shape

Orea: the amount of space inside a shape Perimeter: the length around a shape Regular Polygons: All sides and angles are equal

Quadrilateral Facts





<u>Parallelogram</u> Opposite sides are parallel

Opposite angles are equal Co-interior angles





Opposite angles are equal

Oll sides equal size



Kite

No parallel lines Equal lengths on top sides Equal lengths on bottom One pair of equal angles

YEAR 9 — REASONING WITH GEOMETRY... Rotation & Translation

@whisto maths

What do I need to be able to do?

By the end of this unit you should be able to:

- Identify the order of rotational symmetry
- Rotate a shape about a point on the
- Rotate a shape about a point not on a
- Translate by a given vector
- Compare rotations and reflections

Keywords

Rotate: a rotation is a circular movement

Symmetry: when two or more parts are identical after a transformation.

Reaular: a regular shape has angles and sides of equal lengths. **Invariant**: a point that does not move after a transformation.

Vertex: a point two edges meet.

Horizontal: from side to side

Vertical: from up to down

Tracing paper helps check Rotational Symmetry rotational symmetry I. Trace your shape (mark the centre point) 2. Rotate your tracing paper on top of the original through 360° 3. Count the times it fits back into itself

O regular pentagon has rotational symmetry of order 5

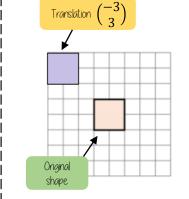
Translation and vector notation

Vector

Notation

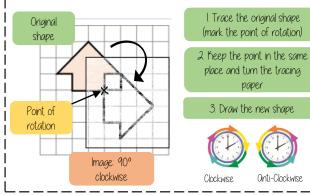
How far left or right to move Negative value (left) Positive value (right)

How far up or down to move Negative value (down) Positive value (up)

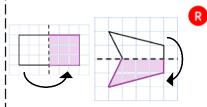


Every vertex has been translated by the same amount

Rotate from a point (in a shape)



Compare rotations and reflections

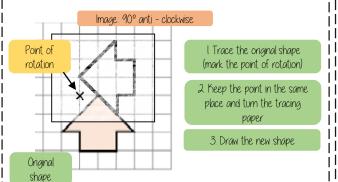


Reflections are a mirror image of the original shape.

Information needed to perform a reflection

- Line of reflection (Mirror line)

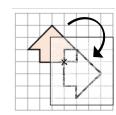
Rotate from a point (outside a shape)



Rotations are the movement of a shape in a circular motion

Information needed to perform a rotation:

- Point of rotation
- Direction of rotation
- Degrees of rotation



YEAR 9 — REASONING WITH GEOMETRY... Pythagoras' theorem

What do I need to be able to do?

By the end of this unit you should be able to:

- Use square and cube roots
- Identify the hypotenuse
- Calculate the hupotenuse
- Find a missing side in a Right angled
- Use Pythagoras' theorem on axes
- Explore proofs of Pythagoras' theorem.

Keywords

Square number: the output of a number multiplied by itself

Square root: a value that can be multiplied by itself to give a square number

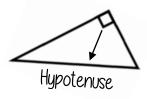
Hupotenuse: the largest side on a right angled triangle. Olways opposite the right angle.

Opposite: the side opposite the anale of interest

Odjacent: the side next to the angle of interest

Squares and square roots is the square root symbol This can also be written as 6^2 eg $\sqrt{64} = 8$ Because 8 × 8 = 64 5 × 5 10 × 10 4 16 25 36 49 64 81 100 Square numbers

Identify the hypotenuse



If a triangle is right-angled, the sum of the squares of the shorter sides will equal the square of the hypotenuse.

Determine if a triangle is right-angled

 $a^2 + b^2 = \text{hypotenuse}^2$

eq $a^2+b^2 = hypotenuse^2$

 $3^2 + 4^2 = 5^2$

9 + 16 = 25

Substituting the numbers into the theorem shows that this is a right-angled triangle

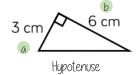
The hypotenuse is always the longest side on a triangle because it is opposite the biggest angle.



Polygons can still have a hypotenuse if it is split up into 1 triangles and opposite a right

Calculate the hypotenuse

a = 3 b = 4



Either of the short sides can be labelled a or b

 $a^2 + b^2 = \text{hypotenuse}^2$

I Substitute in the values for a and b

 3^2+6^2 = hypotenuse²

 $9 + 36 = \text{hypotenuse}^2$

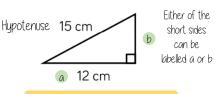
 $45 = hypotenuse^2$

2. To find the hypotenuse square root the sum of the squares of the shorter sides.

 $\sqrt{45}$ = hypotenuse

6.71cm = hypotenuse

Calculate missing sides



 $a^2 + b^2 = \text{hypotenuse}^2$

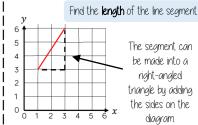
 $12^2 + b^2 = 15^2$ I Substitute in the values you are given

 $144 + b^2 = 225$

Rearrange the equation by subtracting the shorter square from the hypotenuse squared

 $b^2 = 111$ Square root to find the length $b = \sqrt{111} = 10.54 \ cm$ of the side

Pythagoras' theorem on a coordinate axis



The line segment is the hypotenuse

 $a^2 + b^2 = \text{hypotenuse}^2$

The lengths of a and b are the sides of the triangle.

Be careful to check the scale on the axes