

Working in the Cartesian plane

What you need to be able to do?

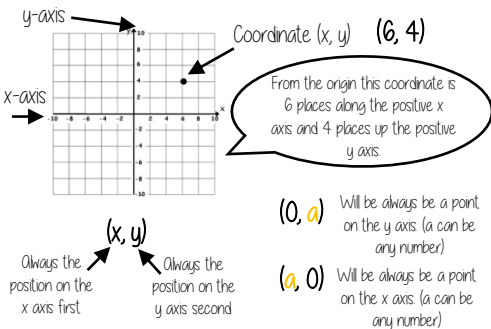
By the end of this unit you should be able to:

- Label and identify lines parallel to the axes
- Recognise and use basic straight lines
- Identify positive and negative gradients
- Link linear graphs to sequences
- Plot $y = mx + c$ graphs

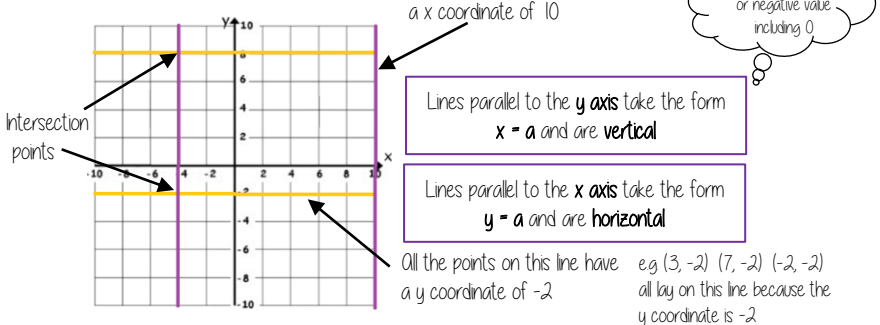
Keywords

- Quadrant:** four quarters of the coordinate plane.
- Coordinate:** a set of values that show an exact position
- Horizontal:** a straight line from left to right (parallel to the x axis)
- Vertical:** a straight line from top to bottom (parallel to the y axis)
- Origin:** (0,0) on a graph. The point the two axes cross
- Parallel:** Lines that never meet
- Gradient:** The steepness of a line
- Intercept:** Where lines cross

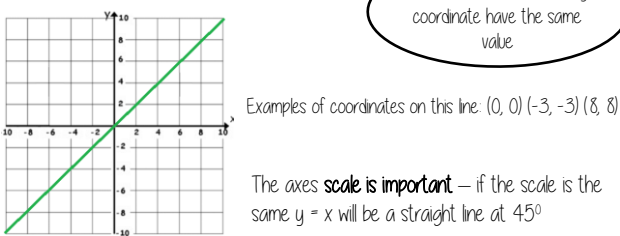
Coordinates in four quadrants



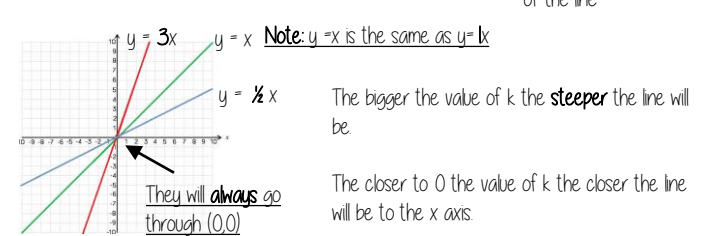
Lines parallel to the axes



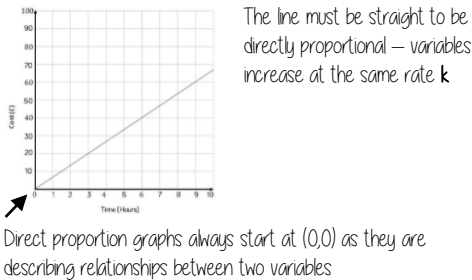
Recognise and use the line $y=x$



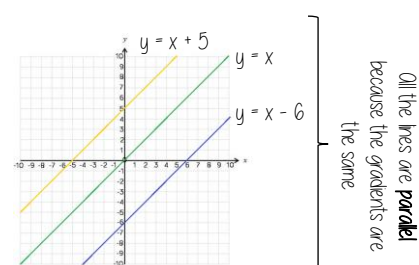
Recognise and use the lines $y=kx$



Direct Proportion using $y=kx$



Lines in the form $y = x + a$

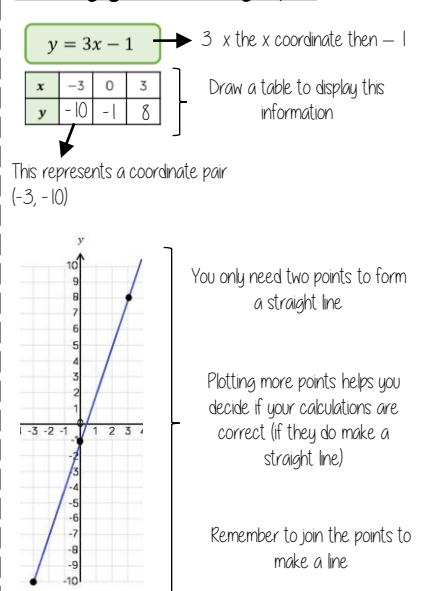


This is the line $y=x$ when the y and x coordinate are the same

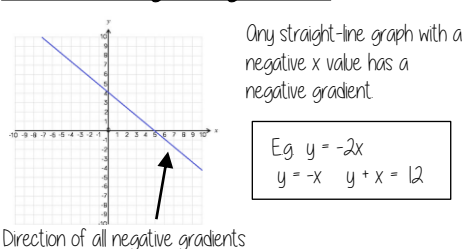
This shows the translation of that line. e.g $y = x + 5$ is the line $y=x$ moved 5 places up the graph

5 has been added to each of the x coordinates

Plotting $y = mx + c$ graphs



Lines with negative gradients



Fractions & Percentages

@ What do I need to be able to do?

By the end of this unit you should be able to:

- Convert between FDP less than and more than 100.
- Increase or decrease using multipliers.
- Express an amount as a percentage.
- Find percentage change.

Keywords

- Percent:** parts per 100 – written using the % symbol
- Decimal:** a number in our base 10 number system. Numbers to the right of the decimal place are called decimals.
- Fraction:** a fraction represents how many parts of a whole value you have.
- Equivalent:** of equal value.
- Reduce:** to make smaller in value.
- Growth:** to increase/ to grow.
- Integer:** whole number, can be positive, negative or zero.
- Invest:** use money with the goal of it increasing in value over time (usually in a bank).

Convert FDP



70/100 → This also means 70 out of 100 squares → 70 "hundredths" = 7 "tenths" = 0.7 → 70 hundredths = - 70%

Using a calculator → → S-D → Convert to a decimal → × 100 converts to a percentage

This will give you the answer in the simplest form

Be careful of recurring decimals

eg $\frac{1}{3} = 0.333333$

$\frac{3}{3} = 0.\dot{3}$

The dot above the 3

Fraction/ Percentage of amount



Find $\frac{3}{5}$ of £60

← £60 →

 ← £36 →

Remember $\frac{3}{5} = 60\% = 0.6$

10% of £60 = £6
 50% of £60 = £30
 60% of £60 = £36

Remember $\frac{3}{5} = 60\% = 0.6$
 60% of £60 = 0.6 × 60 = £36

Convert FDP < and > 100%

100 hundredths = 10 tenths = 100% → 40 hundredths = 4 tenths = 40%

140 hundredths = 14 tenths = 140%

100% + 40%
 1 + 0.40
 = 1.40

Percentage decrease: Multipliers

← 100% →

 ← 42% → Decrease by 58%

$100\% - 58\% = 42\%$
 $100 - 58 = 42$

Multiplier Less than 1

Percentage increase: Multipliers

← 100% → → 12% →

 Increase by 12%

$100\% + 12\% = 112\%$
 $100 + 12 = 112$

Multiplier More than 1

Express as a % - Non-calculator

7 per every 10 are orange → This means that 70 per every 100 are orange → $\frac{70}{100}$ → 70%

$\frac{7}{10}$

27 per every 50 shaded → 54 per every 100 shaded → 54%

$\frac{27}{50}$ → $\frac{54}{100}$

Denominator 100 Equivalent fractions

Express as a % - Calculator

Rosie

$\frac{13}{30}$ → $\frac{13}{30}$ → × 100 → 43.333...% → 43%

Can't use equivalence easily to find 'per hundred'

This is the same as 13 ÷ 30

Decimal percentages are still a percentage.

Percentage change

I bought a phone for £200. A year later sold it for £125.

← 100% →

 ← 75% →

All values of change compare to the ORIGINAL value

Percentage loss
 $\frac{75}{200} \times 100 = 37.5\%$

$\frac{\text{Difference in value}}{\text{Original value}} \times 100$

I bought a house for £180,000, I later sold it for £216,000.

← 100% →

 ← 20% →

Percentage profit
 $\frac{36000}{180000} \times 100 = 20\%$

Money made (profit value)

Choose appropriate method

The language and wording of the question is the key

Have you represented the question in a bar model?
 Can you use a calculator?

Brackets, Equations & Inequalities

What you need to be able to do?

By the end of this unit you should be able to:

- Form Expressions
- Expand and factorise single brackets
- Form and solve equations
- Solve equations with brackets
- Represent inequalities
- Form and solve inequalities

Keywords

- Simplify:** grouping and combining similar terms
- Substitute:** replace a variable with a numerical value
- Equivalent:** something of equal value
- Coefficient:** a number used to multiply a variable
- Product:** multiply terms
- Highest Common Factor (HCF):** the biggest factor (or number that multiplies to give a term)
- Inequality:** an inequality compares two values showing if one is greater than, less than or equal to another

Form expressions

For unknown variables, a letter is normally used in its place


More than - ADD

Less than/ difference - SUBTRACT

e.g. 4 more than t \longrightarrow $t + 4$
 8 less than k \longrightarrow $k - 8$

Only similar terms can be grouped together

e.g. Find the perimeter of this shape
 (Perimeter = length around outside of shape)



$t + 2t + 1 + t + 2t + 1 \longrightarrow 6t + 2$

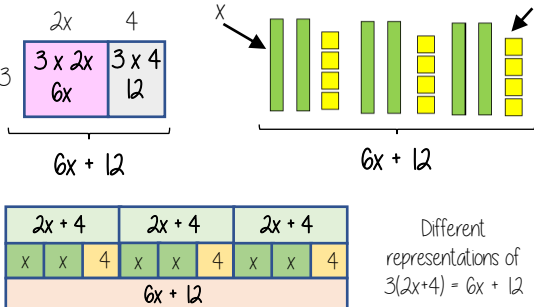
Directed numbers

- $++ \longrightarrow +$
- $-- \longrightarrow +$
- $+ - \longrightarrow -$
- $- + \longrightarrow -$

e.g. $a = -5$ and $b = 2$
 $a^2 = a \times a = -5 \times -5 = 25$
 $b + a = 2 + -5 = -3$

Multiply single brackets

$3(2x + 4)$



Area model: $3 \times 2x = 6x$, $3 \times 4 = 12$, total $6x + 12$.

Bar model: $3(2x + 4) = 6x + 12$.

Different representations of $3(2x+4) = 6x + 12$

Factorise into a single bracket

$8x + 4$



Try and make this the highest common factor

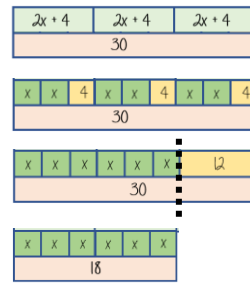
The two values multiply together (also the area) of the rectangle

$8x + 4 \equiv 4(2x + 1)$

Note:
 $8x + 4 \equiv 2(4x + 2)$
 This is factorised but the HCF has not been used

Solve equations with brackets

$3(2x + 4) = 30$



30

30

30

18

$3(2x + 4) = 30$

Expand the brackets

$6x + 12 = 30$

-12

$6x = 18$

-6

Substitute to check your answer.
 This could be negative or a fraction or decimal

$x = 3$

Simple Inequalities

- $<$ less than
- \leq Less than or equal to
- $>$ More than
- \geq More than or equal to

$x < 10$

Say this out loud
 "x is a value less than 10"

$10 > x$

Say this out loud
 "10 is more than the value"

Note:
 $x < 10$ and $10 > x$
 represent the same values

$x + 2 \leq 20$

"my value + 2 is less than or equal to 20"

$x \leq 18$

The biggest the value can be is 18

Form and solve inequalities



Two more than treble my number is greater than 11

Find the possible range of values

Form

$x \longrightarrow x3 \longrightarrow +2 \longrightarrow 11$

$3x + 2 > 11$

Solve

$x \longleftarrow -3 \longleftarrow -2 \longleftarrow 11$

$x > 3$

Check

This would suggest any value bigger than 3 satisfies the statement

$3 \times 3 + 2 = 11 \checkmark$

$10 \times 3 + 2 = 32 \checkmark$

Algebraic constructs

Expression

A sentence with a minimum of two numbers and one maths operation

Equation

A statement that two things are equal

Term

A single number or variable

Identity

An equation where both sides have variables that cause the same answer includes \equiv

Formula

A rule written with all mathematical symbols e.g. area of a rectangle $A = b \times h$

Standard Form

What do I need to be able to do?

By the end of this unit you should be able to:

- Write numbers in standard form and as ordinary numbers
- Order numbers in standard form
- Add/ Subtract with standard form
- Multiply/ Divide with standard form
- Use a calculator with standard form

Keywords

Standard (index) Form: A system of writing very big or very small numbers

Commutative: an operation is commutative if changing the order does not change the result.

Base: The number that gets multiplied by a power

Power: The exponent — or the number that tells you how many times to use the number in multiplication

Exponent: The power — or the number that tells you how many times to use the number in multiplication

Indices: The power or the exponent

Negative: A value below zero.

Positive powers of 10

1 billion = 1 000 000 000

$$10 \times 10 \times 10 \times 10 \times 10 \times 10 \times 10 \times 10 \times 10 \times 10 = 10^9$$

Addition rule for indices $10^a \times 10^b = 10^{a+b}$

Subtraction rule for indices $10^a \div 10^b = 10^{a-b}$

Standard form with numbers > 1

Any number between 1 and less than 10 $\rightarrow A \times 10^n$ ← Any integer

Example

$$3.2 \times 10^4$$

$$= 3.2 \times 10 \times 10 \times 10 \times 10$$

$$= 32000$$

Non-example

0.8×10^4

5.3×10^{07}

Negative powers of 10

0.001	10	1	$\frac{1}{10}$	$\frac{1}{100}$	$\frac{1}{1000}$
$1 \times \frac{1}{1000}$	10^1	10^0	10^{-1}	10^{-2}	10^{-3}
1×10^{-3}	0	0	0	0	1

Any value to the power 0 always = 1

Negative powers do not indicate negative solutions

Numbers between 0 and 1

0.054 = 5.4×10^{-2}

1	$\frac{1}{10}$	$\frac{1}{100}$	$\frac{1}{1000}$
10^0	10^{-1}	10^{-2}	10^{-3}
0	0	5	4

A negative power does not mean a negative answer — it means a number closer to 0

Order numbers in standard form

6.4×10^{-2}	2.4×10^2	3.3×10^0	1.3×10^{-1}
0.064	240	1	0.13

Look at the power first will the number be = > or < than 1

Use a place value grid to compare the numbers for ordering

Mental calculations

$6.4 \times 10^2 \times 1000$ Not in Standard Form

= $6.4 \times 10^2 \times 10^3$

Use addition for indices rule

= 6.4×10^5

$(2 \times 10^3) \div 4$

Divide the values

= $(2 \div 4) \times 10^3$

= 0.5×10^3

$8 \times 10^5 \times 3$

= 24×10^5 Not in Standard Form

Use addition for indices rule

= $2.4 \times 10^1 \times 10^5$

= 2.4×10^6

Remember the layout for standard form

Any number between 1 and less than 10 $\rightarrow A \times 10^n$ ← Any integer

Addition and Subtraction

Tip: Convert into ordinary numbers first and back to standard form at the end

Method 1

= 600000 + 800000

= 1400000

= 1.4×10^6

$6 \times 10^5 + 8 \times 10^5$

Method 2

= $(6 + 8) \times 10^5$

= 14×10^5

= $1.4 \times 10^1 \times 10^5$

= 1.4×10^6

This is not the final answer

More robust method
Less room for misconceptions
Easier to do calculations with negative indices
Can use for different powers

Only works if the powers are the same

Multiplication and division

$\frac{1.5 \times 10^5}{0.3 \times 10^3}$ ← Division questions can look like this

For multiplication and division you can look at the values for A and the powers of 10 as two separate calculations

$(1.5 \times 10^5) \div (0.3 \times 10^3)$

$15 \div 0.3 \times 10^5 \div 10^3$

Revisit addition and subtraction laws for indices — they are needed for the calculations

= 5×10^2

Addition law for indices
 $a^m \times a^n = a^{m+n}$

Subtraction law for indices
 $a^m \div a^n = a^{m-n}$

Using a calculator

$14 \times 10^5 \times 3.9 \times 10^3$

Use a calculator to work out this question to a suitable degree of accuracy

Input 14 and press $\times 10^1$ Then press 5 (for the power)

Press \times

Input 3.9 and press $\times 10^3$ Then press 3 (for the power)

Press $=$

This gives you the solution



Click calculator for video tutorial

To put into standard form and a suitable degree of accuracy

Press **SHIFT** **SETUP** and then press 7 for sci mode

Choose a degree of accuracy so in most cases press 2

Answer: 5.5×10^8

YEAR 8

Applying number

What do I need to be able to do?

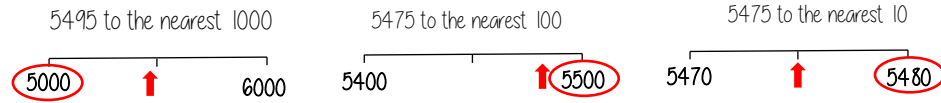
By the end of this unit you should be able to:

- Round numbers to powers of 10 and 1 sf
- Round numbers to any dp
- Estimate solutions
- Calculate using order of operations
- Calculate with money, units of measurement and time

Keywords

- Significant:** Place value of importance
Round: Making a number simpler but keeping its value close to what it was
Decimal: Place holders after the decimal point
Overestimate: Rounding up – gives a solution higher than the actual value
Underestimate: Rounding down – gives a solution lower than the actual value
Metric: A system of measurement
Balance: The amount of money in a bank account
Deposit: Putting money into a bank account

Round to powers of 10 and 1 sig figure R If the number is halfway between we "round up"



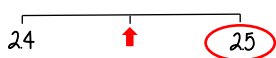
- 370 to 1 significant figure is 400
- 37 to 1 significant figure is 40
- 3.7 to 1 significant figure is 4
- 0.37 to 1 significant figure is 0.4
- 0.00037 to 1 significant figure is 0.0004

Round to the first non-zero number

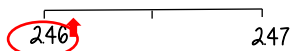
Round to decimal places R

"To 1dp" – to one number after the decimal
 "To 2dp" – to two numbers after the decimal

2.46192 (to 1dp) - Is this closer to 2.4 or 2.5



2.46192 (to 2dp) - Is this closer to 2.46 or 2.47



Focus on the numbers after the decimal point

2.46192 This shows the number is closer to 2.5

2.46192 This shows the number is closer to 2.46

Estimate the calculation

Round to 1 significant figure to estimate

$$4.2 + 6.7 \approx 4 + 7 \approx 11$$

This is an **overestimate** because the 6.7 was rounded up more

The equal sign changes to show it is an estimation

$$214 \times 3.1 \approx 20 \times 3 \approx 60$$

This is an **underestimate** because both values were rounded down

It is good to check all calculations with an estimate in all aspects of maths – it helps you identify calculation errors

Order of operations R

Brackets Operations in brackets are calculated first

Other operations e.g powers, roots,

Multiplication/ Division

They are carried out in the order from left to right in the question

Addition/ Subtraction

They are carried out in the order from left to right in the question

Calculations with money

Debit - You have £0 or more in an account

Credit - You have less than £0 in an account

Money calculations are to 2dp



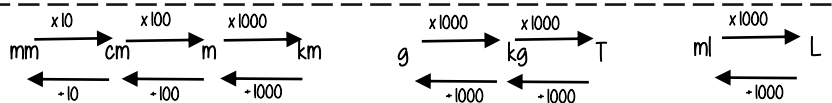
Using a calculator – ensure you are working in the correct units

$$\begin{aligned} \text{£ } 1.30 + 50\text{p} &= 1.30 + 0.50 \quad (\text{in pence}) \\ &= 1.30 + 0.50 \quad (\text{in pounds}) \end{aligned}$$

$$\text{£ } 1 = 100\text{p}$$



Units are important: Useful Conversions



Metric measures of length

$$\text{Kilo} = 1000 \times \text{meter} \quad \text{Centi} = \frac{1}{100} \times \text{meter}$$

$$\text{Milli} = \frac{1}{1000} \times \text{meter}$$

Units of weight/ capacity

Weight = g, kg, t
 Capacity (volume of liquid) = ml, L

Time and the calendar

1 Year – the amount of time it takes Earth to go around the sun **365** (and a quarter) days
Leap Year – **366** days (every 4 years)



12 Months – one year = 52 weeks
 31 days – Jan, March, May, July
 30 days – April, June, Sept, Nov
 28 days – Feb (29 leap year)

1 week – 7 days
 Monday, Tuesday, Wednesday
 Thursday, Friday, Saturday, Sunday

1 day – 24 hours
1 hour – 60 minutes
1 minute – 60 seconds

Use a number line for time calculations!

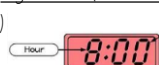
Analogue Clock



12-hour clock

- Use am (morning) and pm (afternoon)
- Only use hour times up to 12

Digital Clock (24-hour times)



24-hour clock

- 0-11 (morning hours)
- 12-23 (afternoon hours)